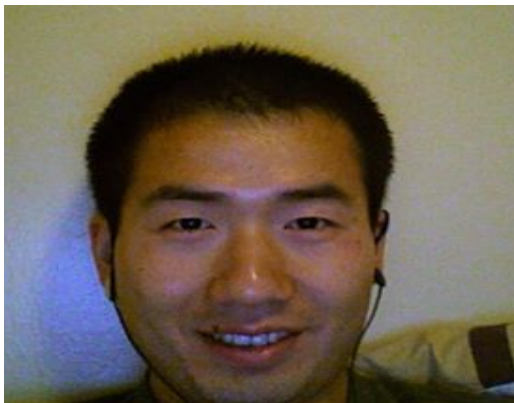
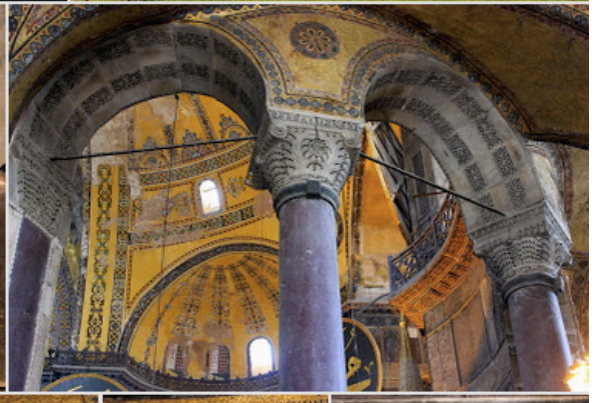
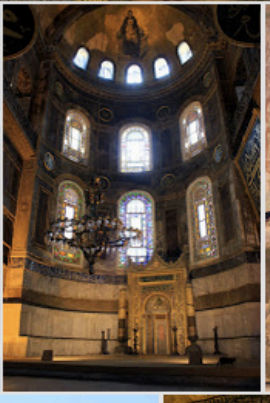
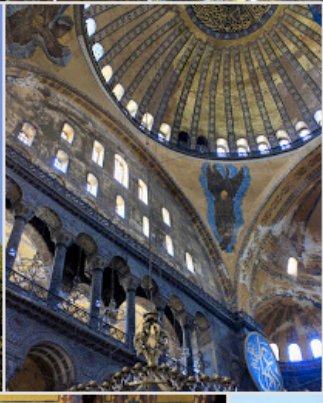
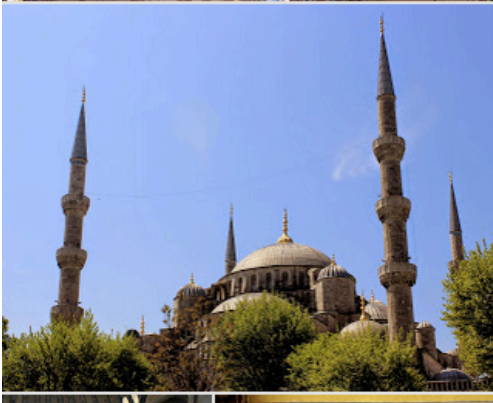
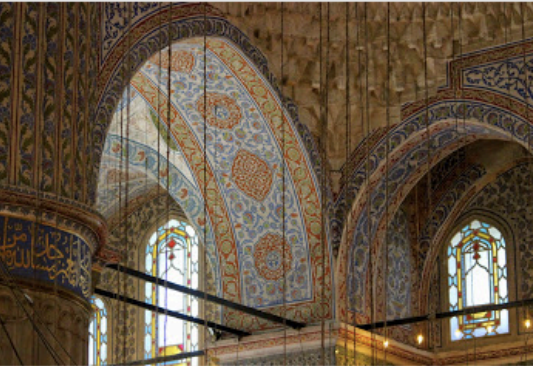
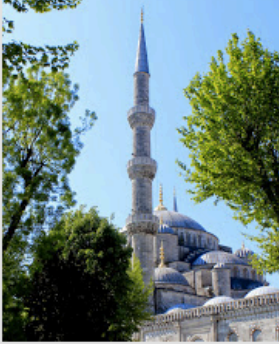


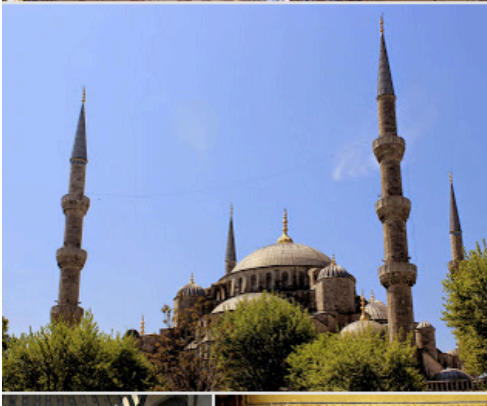
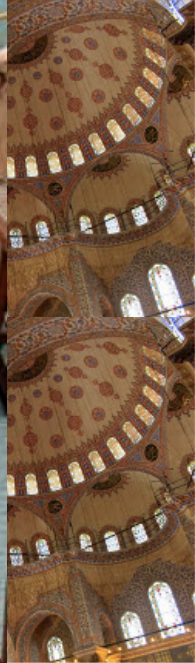


# Capability Models and Their Applications in Planning

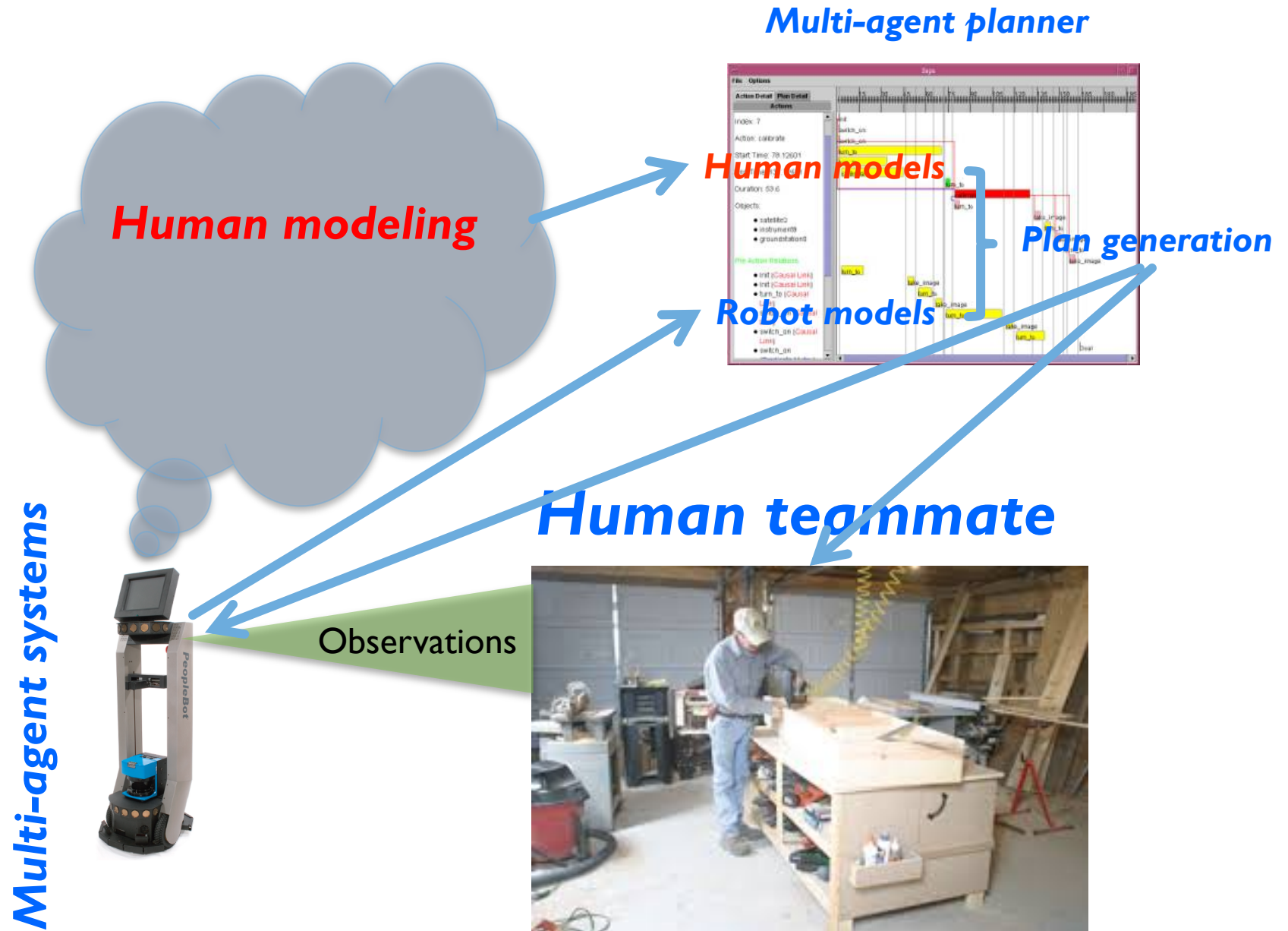
**Yu Zhang, Sarath Sreedharan &  
Subbarao Kambhampati**  
**Arizona State University**







# Planning with Humans in the Loop





# Human-in-the-Loop Planning & Decision Support

AAAI 2015 Tutorial

[rakaposhi.eas.asu.edu/hilp-tutorial](http://rakaposhi.eas.asu.edu/hilp-tutorial)

**Subbarao Kambhampati**

Arizona State University

**Kartik Talamadupula**

IBM T.J. Watson Research Center

Funding from ONR, ARO and NSF  
gratefully acknowledged <sup>1</sup>

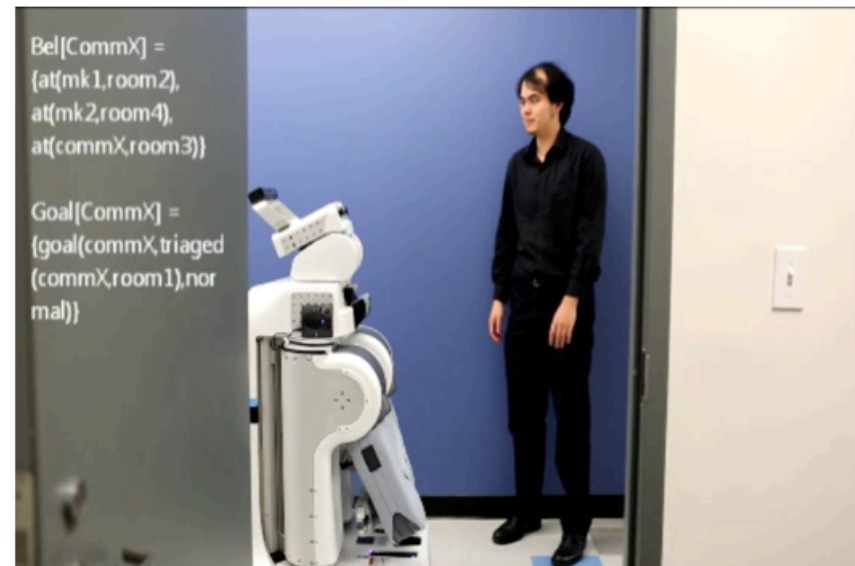
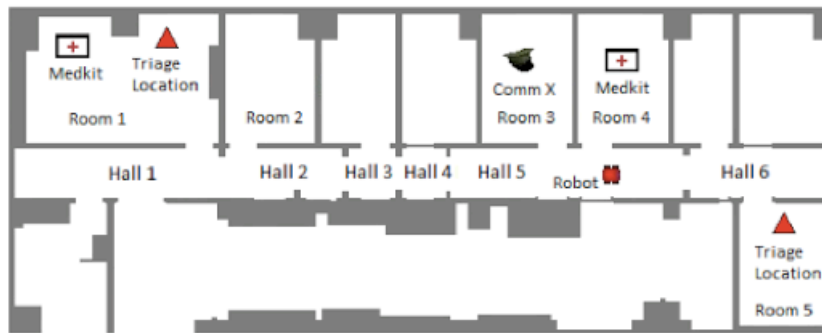


# Interactive Session Paper TuD2.10



## IROS 2014

### COORDINATION IN HUMAN-ROBOT TEAMS USING MENTAL MODELING AND PLAN RECOGNITION



But how do we get the Human Models?



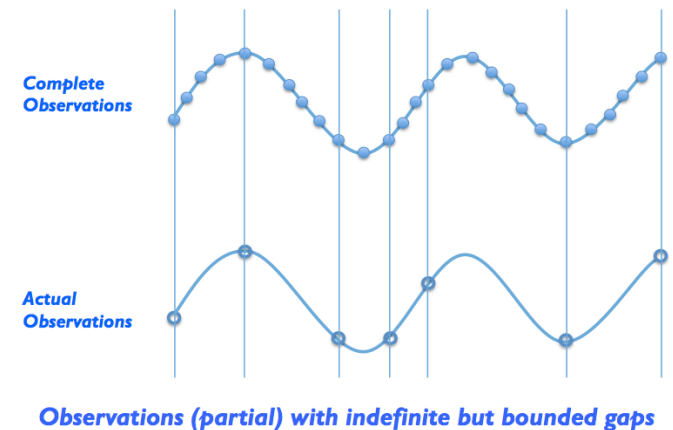
# How do we get the Human Models?

- ◇ Typically multi-agent planning methods assume all agents use similar models
  - ◇ E.g. All agents with STRIPS action models
- ◇ Unreasonable to expect similar sorts of action models for the robot and the human..
  - ◇ Human models (from the Robot's point of view) are likely to be highly incomplete.
- ◇ So how do we represent (and handle) incomplete models of human capabilities?

# Challenges in learning Incomplete Human Models

- ◇ The temptation is to go with existing action models & introduce incompleteness
  - ◇ Atomic: MDP/POMDP
  - ◇ Factored: STRIPS, RDDL, HTN etc
    - ◇ Example work by Garland&Lesh(2002); Nguyen et al (2010, 2014)
- ◇ While they are fine if someone hand-specifies them, they are much harder to learn, given the kinds of information that is likely to be available.
  - ◇ Significant incompleteness in observations
    - ◇ Sensor occlusion, noisy observations,
      - ◇ [Zhuo & Kambhampati, IJCAI 2013]
  - ◇ There may be significant gaps between observations

Our Solution: Capability Models





# Capability

We start with the “default assumption” that domain models are **incomplete**

- **DEFINITION (CAPABILITY)** – Given an agent, a capability is a mapping  $S_\phi \times S_\phi \rightarrow [0, 1]$ , which is an assertion about the probability of the existence of a plan in fewer than or equal to  $T$  atomic state changes that can connect the two states.

->: denote an atomic state change

{has\_water(AG), has\_coffee\_beans(AG)}

-> {has\_boiling\_water(AG), has\_coffee\_beans(AG)}

-> {has\_boiling\_water(AG), has\_ground\_coffee\_beans(AG)}

-> {has\_coffee(AG)}

**When  $T = 2$**  { has\_water(AG) => has\_ground\_coffee\_beans(AG)  
has\_boiling\_water(AG) => has\_coffee(AG)...

**When  $T = 3$**  { ... (including all capabilities when  $T = 2$ )  
has\_water(AG) => has\_coffee(AG)

**Partial states**

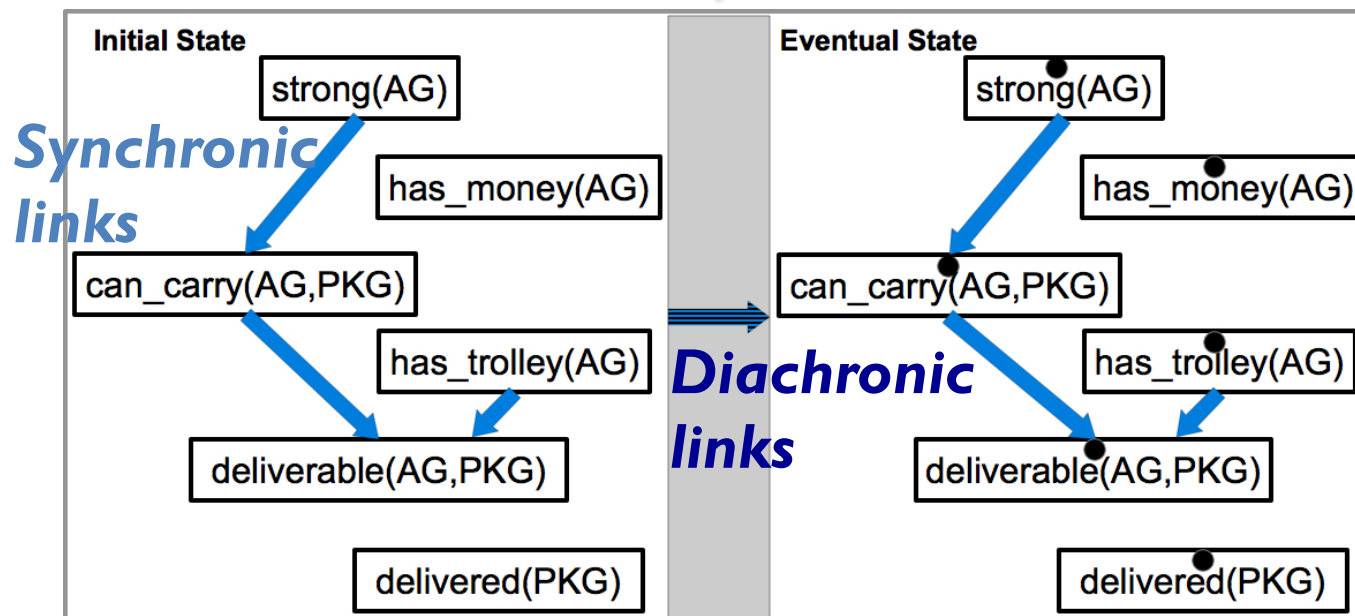
**Bound on the gaps between observations**

# Capability Model

*Capability model encodes all capabilities for a given T*

(Generalization of 2-TBN model used in RDDDL)

*T-gap capability model*

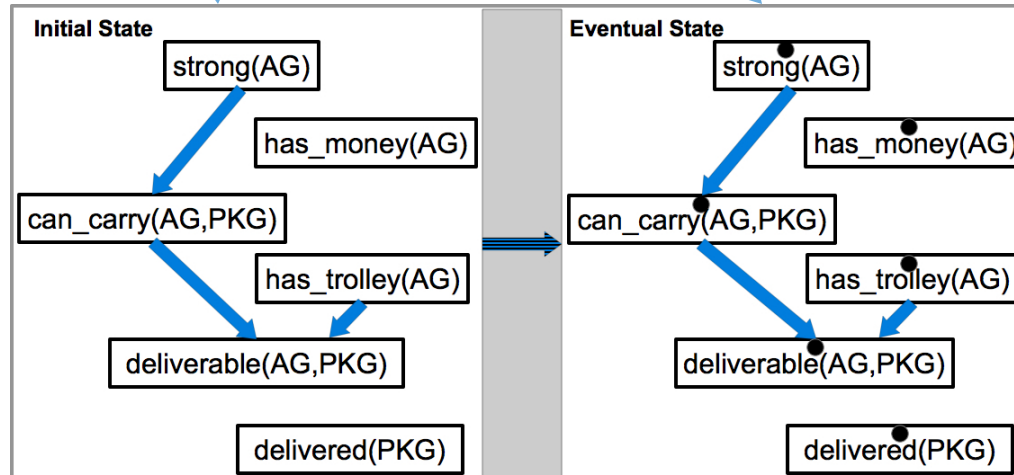


(Imperfect analogy to) HTN Models. A capability can be thought of as an abstract task

# Capability Model

**DEFINITION 3 (CAPABILITY MODEL).** A *capability model* of an agent  $\phi$ , as a binomial ABN  $(G_\phi, F, \rho)$ , has the following specifications:

- $V_\phi = X_\phi \cup \dot{X}_\phi$ .
- $\forall V_i \in V_\phi$ , the domain of  $V_i$  is  $D(V_i) = \{true, false\}$ .
- $\forall V_i \in V_\phi$ ,  $F_i = \{F_{i1}, F_{i2}, \dots\}$ , and each  $F_{ij}$  is a root and has a density function  $\rho_{ij}(f_{ij})$  ( $0 \leq f_{ij} \leq 1$ ). (For each value  $pa_{ij}$  of the parents  $P A_i$ , there is an associated variable  $F_{ij}$ .)
- $\forall V_i \in V_\phi$ ,  $P(V_i = true | pa_{ij}, f_{i1}, \dots, f_{ij}, \dots) = f_{ij}$ .

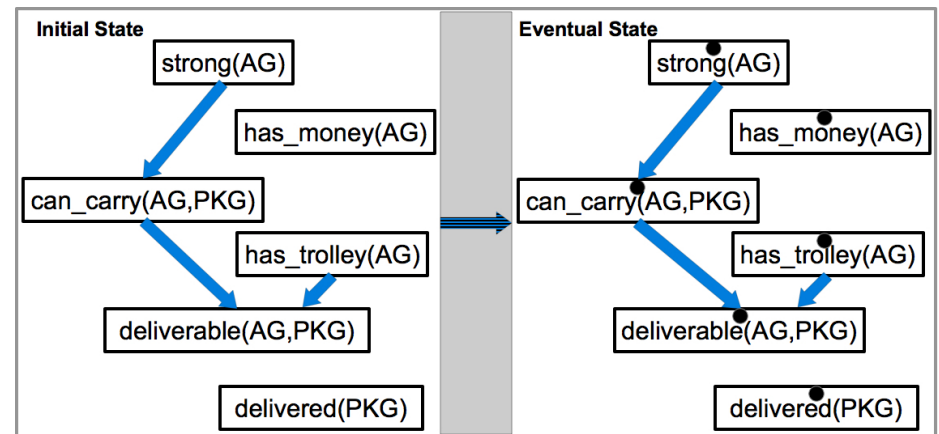


# Capability Model & Encoded Capabilities

**A capability model encodes the following distributions:**

$$P(X_\phi, \dot{X}_\phi) = \int_0^T P(X_\phi, \dot{X}_\phi, t) dt$$

**Joint distribution over  $T$**



**$T$ -gap capability model**

**A capability:**

$$P(\dot{X}_\phi = s_E \mid X_\phi = s_I) \longleftrightarrow s_I \Rightarrow s_E$$

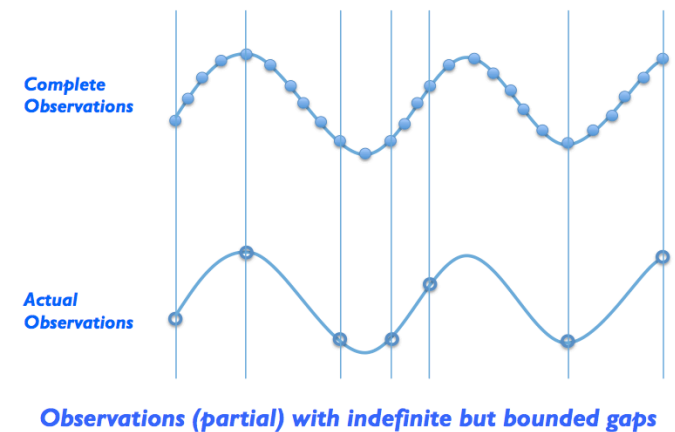
**A conditional probability**

**(specified by a partial initial and eventual state)**

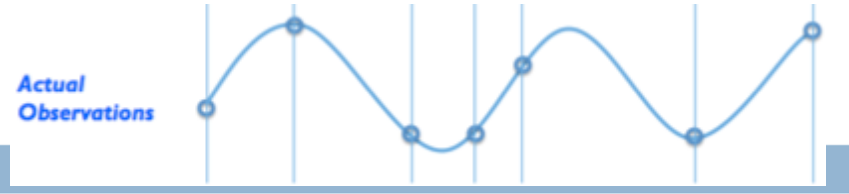
# Learning Capability Models

- Learning model structure      Causal relationships (diachronic links); variable correlations (synchronic links)
- Learning model parameters      Conditional probabilities

## Learning from (gap-bounded) plan traces



# Parameter Learning



**We assume that the maximum number of missing state observations between any two observations in the partial plan trace is upper bounded by  $T$**

**DEFINITION (T-GAP PARTIAL PLAN TRACE).** A T-gap partial plan trace is a partial plan trace in which all  $k_{[1,2,\dots]} \leq T$

$$\mathcal{T} = \langle s_i, s_{i+k_1}, s_{i+k_2}, \dots \rangle$$

Learning samples

Apply Bayesian learning (assuming beta distributions):

$$\rho(f_{ij} | D) = \text{beta}(f_{ij}; a_{ij} + s_{ij}, b_{ij} + t_{ij})$$

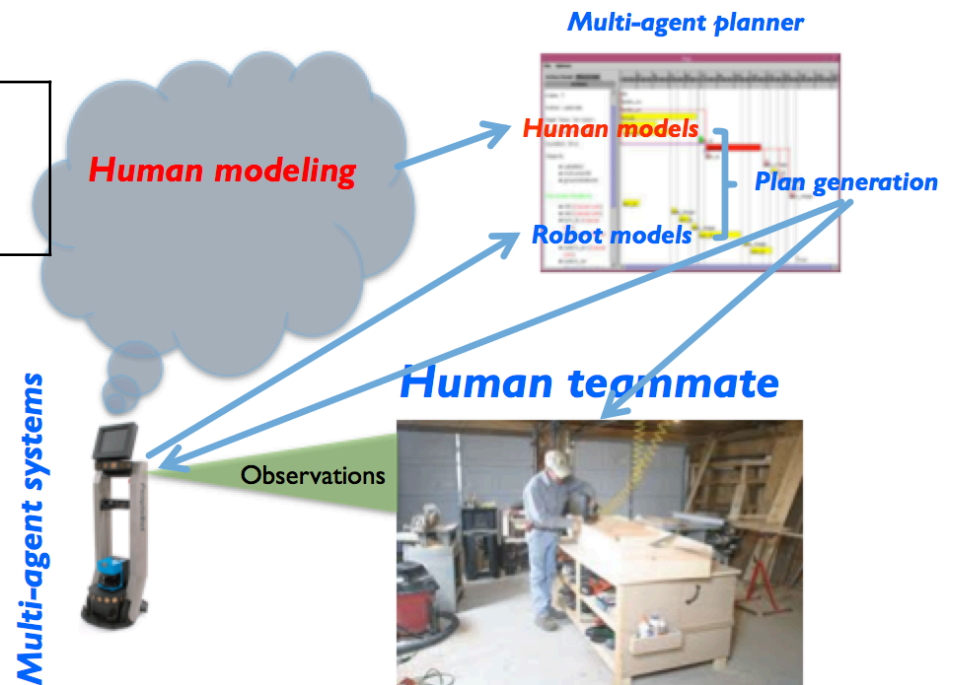
# Using Capability Models

## Single agent planning

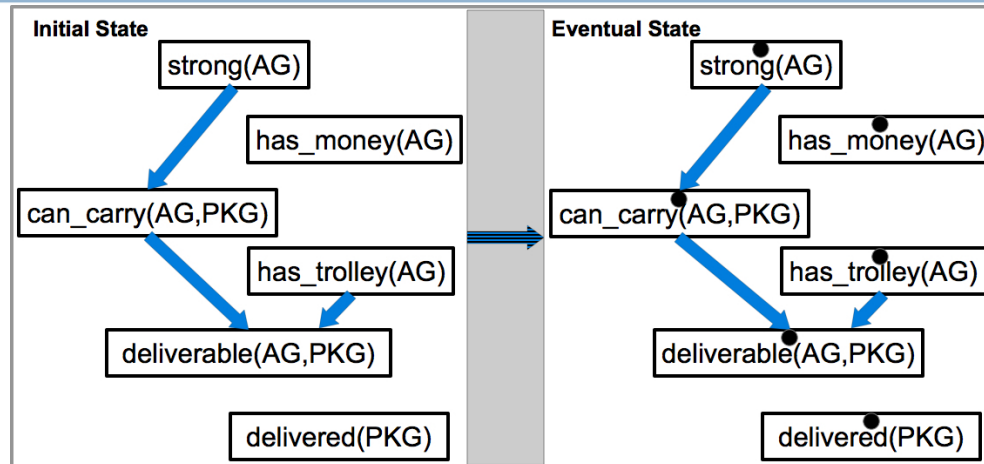
- Robot can reason about whether a human can achieve the task alone

## Multi-agent planning (e.g. Robot and Human)

- Robots can reason about a joint plan with humans



# Planning with Capability Models



## *T-gap capability model*

- Any planning state is a set of complete states: a **belief state**

{(complete state 1), (complete state 2)...}

- Select a capability to apply:  $s_I \Rightarrow s_E = P(\dot{X}_\phi = s_E \mid X_\phi = s_I)$

- For each  $s^*$  in the belief state,

➤ Applicable:  $s_I \sqsubseteq s^*$

Success: compute a set of resulting states  $s$ ,  $s_E \sqsubseteq s$ .

Failure: no change

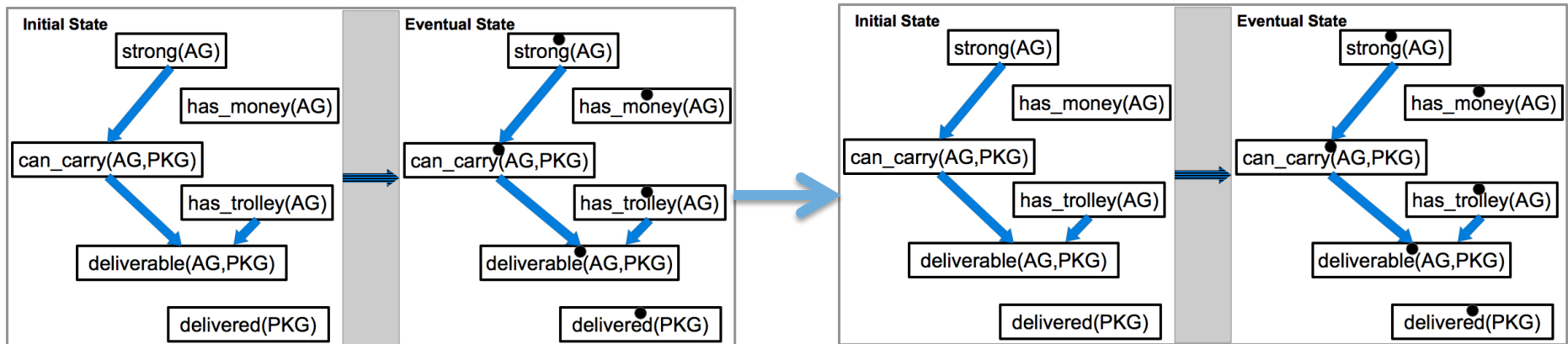
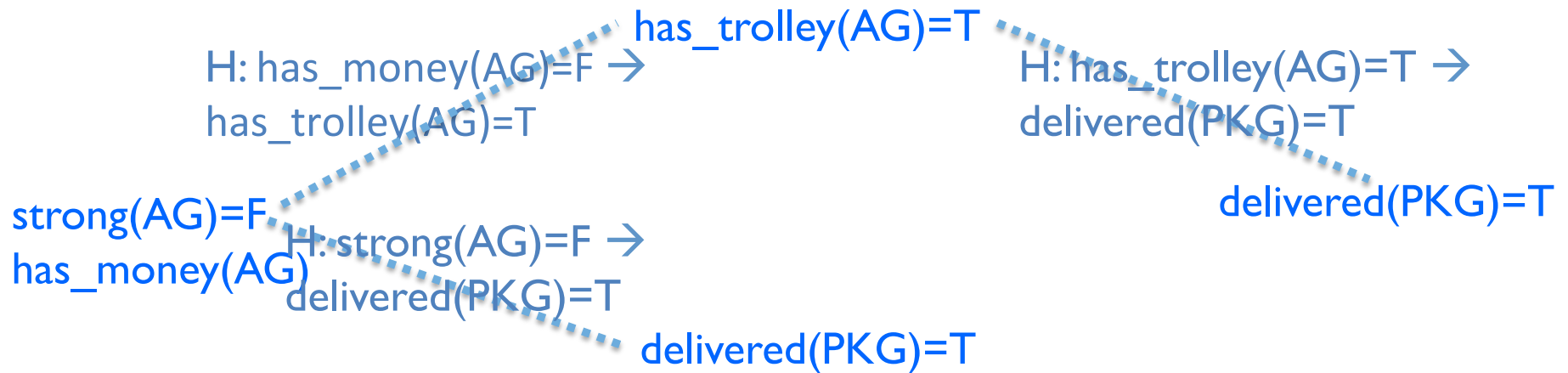
$$P(s) = \frac{P(s^* \Rightarrow s)}{P(s^* \Rightarrow s_E)} = \frac{P(\dot{X}_\phi = s \mid X_\phi = s^*)}{P(\dot{X}_\phi = s_E \mid X_\phi = s^*)}$$

➤ Inapplicable – no change to  $s^*$

$$\sum_{s \in S} P(s) = 1 \quad 21$$



# Single-agent Planning



**Unrolling of 2-gap capability model**

# Single Agent Planning Heuristic

## Assumptions:

$$P(s_I \Rightarrow s_E) \geq P(s'_I \Rightarrow s_E)(T(s'_I) \subseteq T(s_I) \wedge F(s_I) \subseteq F(s'_I))$$

$$P(s_I \Rightarrow s_E) \geq P(s_I \Rightarrow s'_E)(T(s_E) \subseteq T(s'_E) \wedge F(s_E) \subseteq F(s'_E))$$

### **A\* heuristic**

Given any state  $s^*$  in belief state  $b(S)$ :

Compute  $f(s^*) = g(s^*) + h(s^*)$

$g(s^*) =$  cost of capabilities in the plan prefix

The cost of a capability is taken as the negative log of the associated probability

$$h(s^*) = \operatorname{argmax}_{v \in G_s, s_{\sim v}} -\log P(s_{\sim v} \Rightarrow \{v = \text{true}\})$$

- $G_s$  is the set of variables that still need to be made true
- $S_{\sim v}$  is a complete state with all variables being TRUE except for  $v$
- $\{v = \text{true}\}$  is a partial state in which  $v$  is true

$$h(\hat{b}(S)) = \sum_{s \in S} P(s) \cdot h(s)$$

# Multi-agent Planning Problem

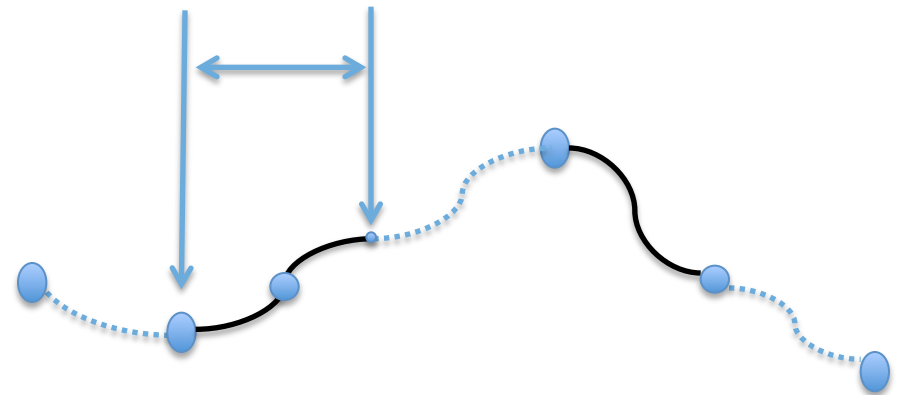
- For robotic agents, we assume STRIPS action models
  - Apply action model on any complete state in the belief state is straightforward
- For human agents, we assume capability models

DEFINITION 8. Given a set of robots  $R = \{r\}$ , a set of human agents  $\Phi = \{\phi\}$ , and a set of typed objects  $O$ , a multi-agent planning problem with mixed models is given by a tuple  $\Pi = \langle \Phi, R, b(\mathcal{I}), G, \rho \rangle$ , where:

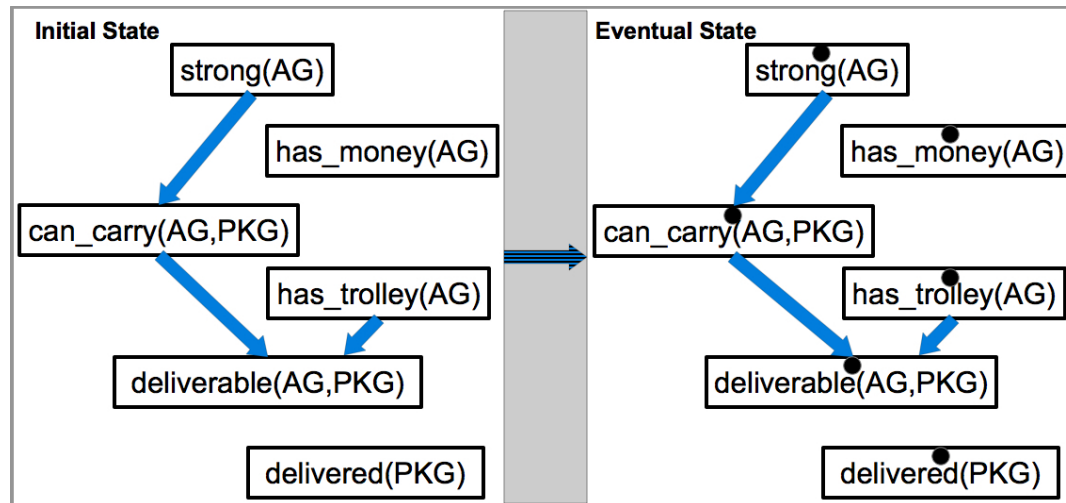
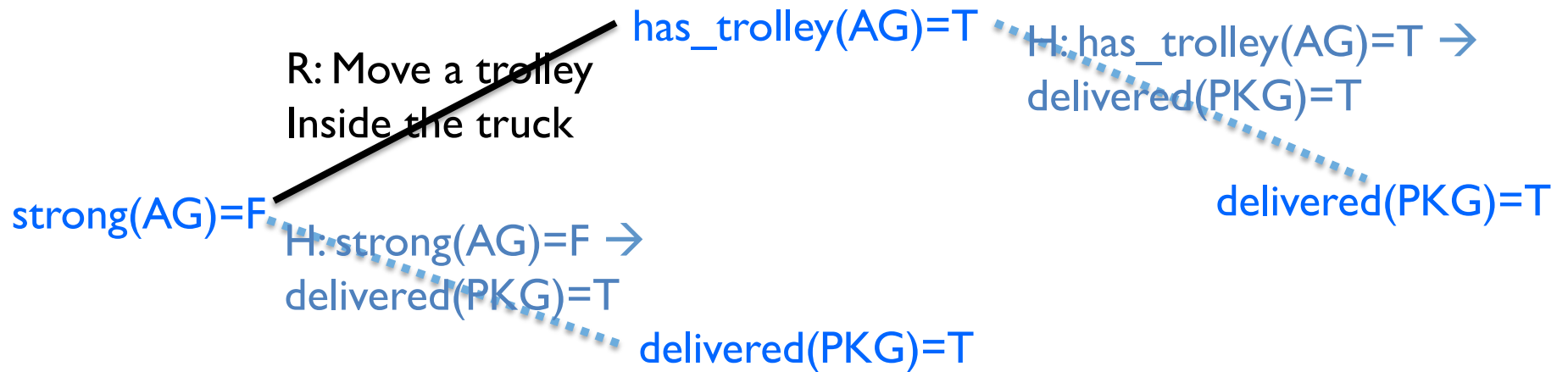
- Each  $r \in R$  is associated with a set of actions  $A(r)$  that are instantiated from  $\mathcal{O}$  and  $O$ , which  $r \in R$  can perform; each action may not always succeed when executed and hence is associated with a cost.
- Each  $\phi \in \Phi$  is associated with a capability model  $G_\phi = \langle V_\phi, E_\phi \rangle$ , in which  $V_\phi = X_\phi \cup \dot{X}_\phi$ .  $X_\phi \subseteq X$ , in which  $X_\phi$  represents the state variables of the world and agent  $\phi$  and  $X$  represents the joint set of state variables of all agents.

## Planning with mixed models!

### Robot actions



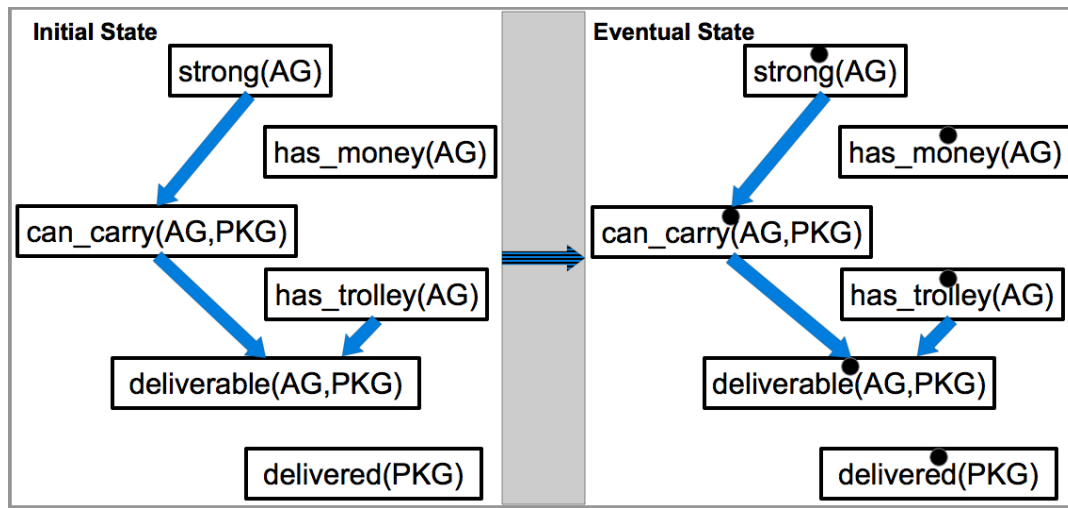
# Multi-agent Planning



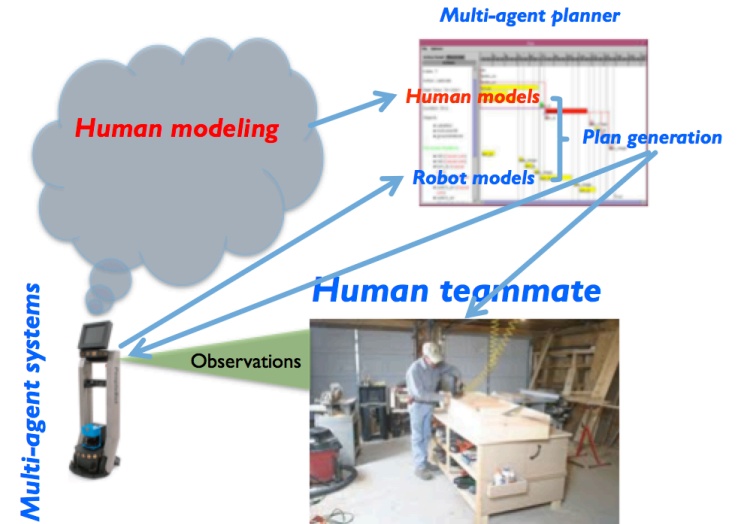
**2-gap capability model**

# Conclusions

- Introduced capability models for human modeling
- Discussed learning and planning with capability models
- Preliminary evaluation in the paper..



**T-gap capability model**



Start with the “default assumption” of **incomplete domains**

- Learn from observations with indefinite but bounded gaps
- Non-angelic uncertainty

➔ **C-plan**